

## Spatially Realistic Monte Carlo Simulations Predict Calcium Dynamics Underlying Transmitter Release at a Neuromuscular Active Zone

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The effect of active zone (AZ) ultrastructure on neurotransmitter release remains poorly understood. A supralinear (~4th order) relationship (*CRR*) between extracellular  $\text{Ca}^{2+}$  ( $[\text{Ca}^{2+}]_o$ ) and transmitter release indicates that multiple  $\text{Ca}^{2+}$  ions are required for fusion of a synaptic vesicle (SV), but how this empirical observation relates to the stoichiometry and architecture of voltage-gated  $\text{Ca}^{2+}$  channels (VGCCs),  $\text{Ca}^{2+}$  binding sites, and SVs is unclear. We created a spatially realistic model of a frog neuromuscular AZ, and used MCCell ([www.mcell.psc.edu](http://www.mcell.psc.edu)) to simulate action potential (AP)-induced  $\text{Ca}^{2+}$  influx through VGCCs,  $\text{Ca}^{2+}$  binding to SVs, and several models of  $\text{Ca}^{2+}$ -dependent SV fusion. We varied spatial parameters to simultaneously reproduce 3 experimental observations: (1) average release probability ( $p_r$ ) per trial per AZ at physiological  $[\text{Ca}^{2+}]_o$ ; (2) the distribution of release latencies ( $L_{dis}$ ); and (3) the 4th order CRR. Also, a 4-state VGCC model reproduced macroscopic  $\text{Ca}^{2+}$  current kinetics, and the on and off rates for  $\text{Ca}^{2+}$  binding were based on the synaptotagmin-1 C2A domain. Given all these constraints, we obtained a surprisingly unique set of model parameters and several counter-intuitive predictions. With a VGCC:SV stoichiometry of 1:1 (supported by other experimental data), each SV contains ~20  $\text{Ca}^{2+}$  binding sites, and 6 sites must be bound simultaneously to induce fusion. Alternative models were either much too  $\text{Ca}^{2+}$ -insensitive to reproduce  $p_r$  or could not simultaneously reproduce  $L_{dis}$  and *CRR*. These results demonstrate the dramatic sensitivity of *CRR*,  $p_r$ , and  $L_{dis}$  to presynaptic architecture, and suggest that vesicle fusion may require a variety of SNARE protein and membrane lipid binding sites for  $\text{Ca}^{2+}$ . Supported by NIH R01 GM068630 (JRS), R01 NS43396 (SDM), P20 GM065805 (JRS), P41 RR06009 (JRS).